

COMSOL  
CONFERENCE



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# Effect of Disintegration of Chemical Stratification on Time-dependent Behavior of the Earth's Mantle

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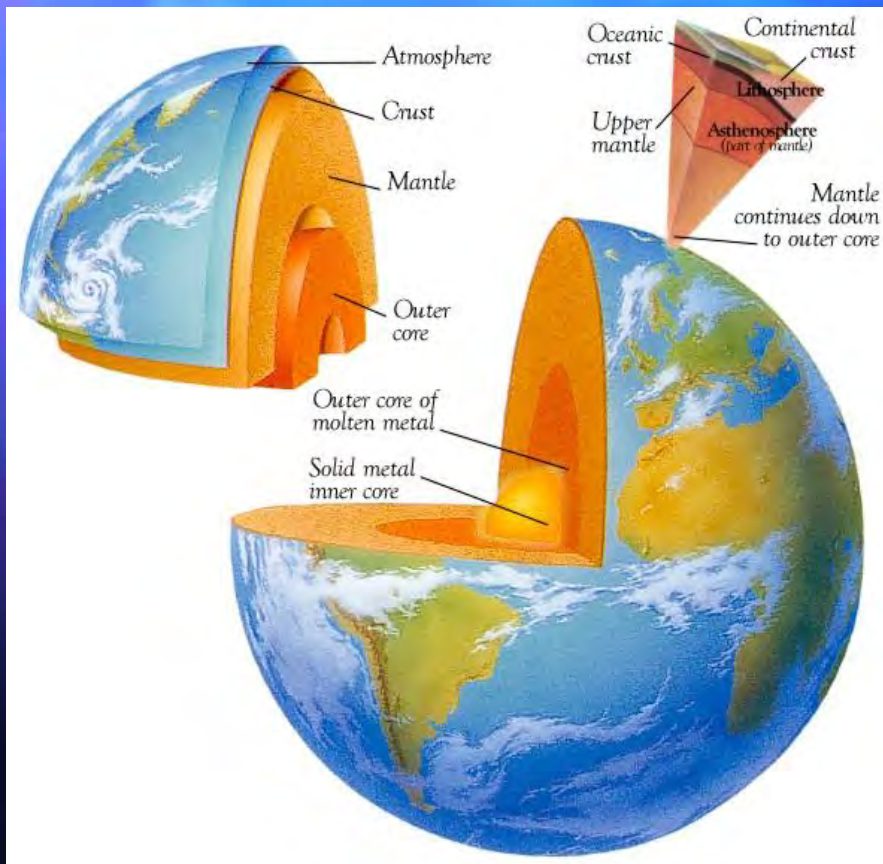
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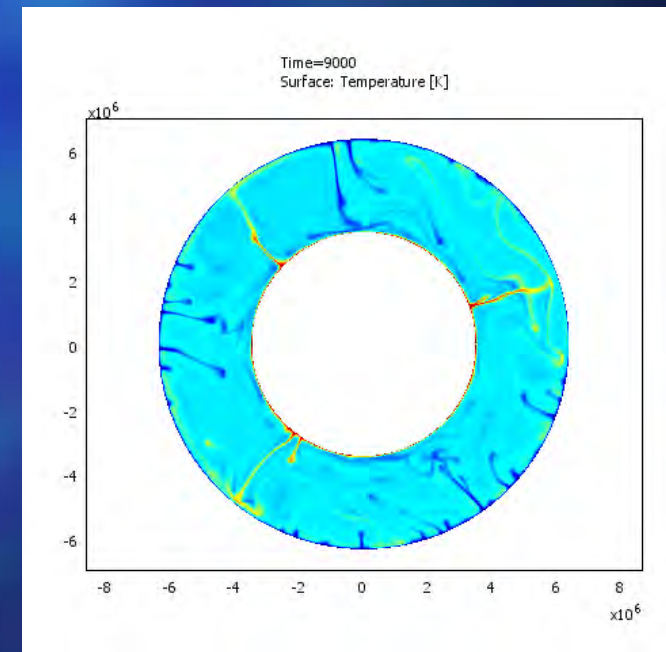
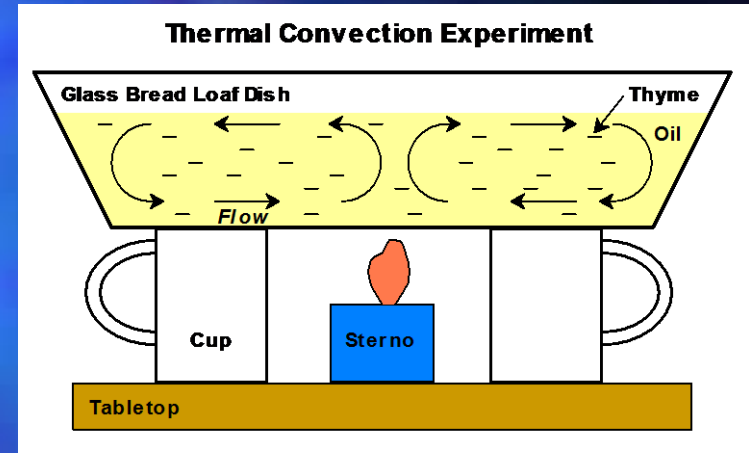
- **Introduction (Earth's structure & mantle convection)**
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# Introduction

## Structure and thermal convection



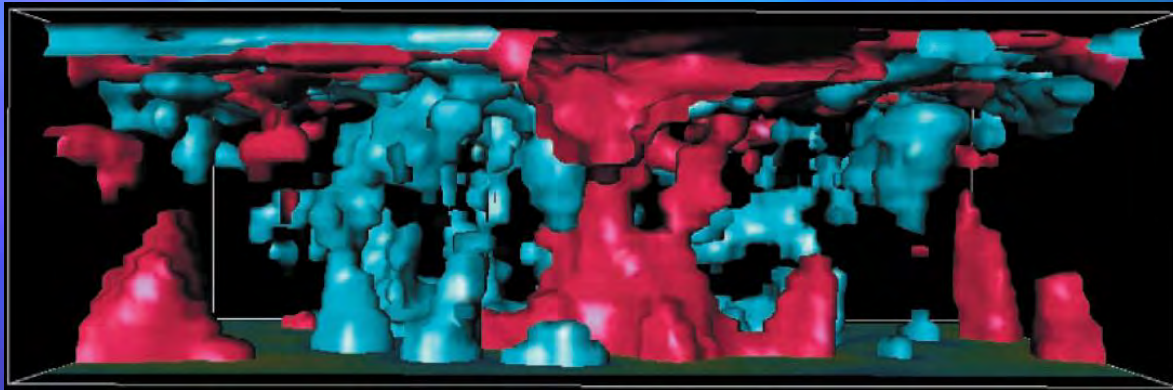
Structure of the Earth



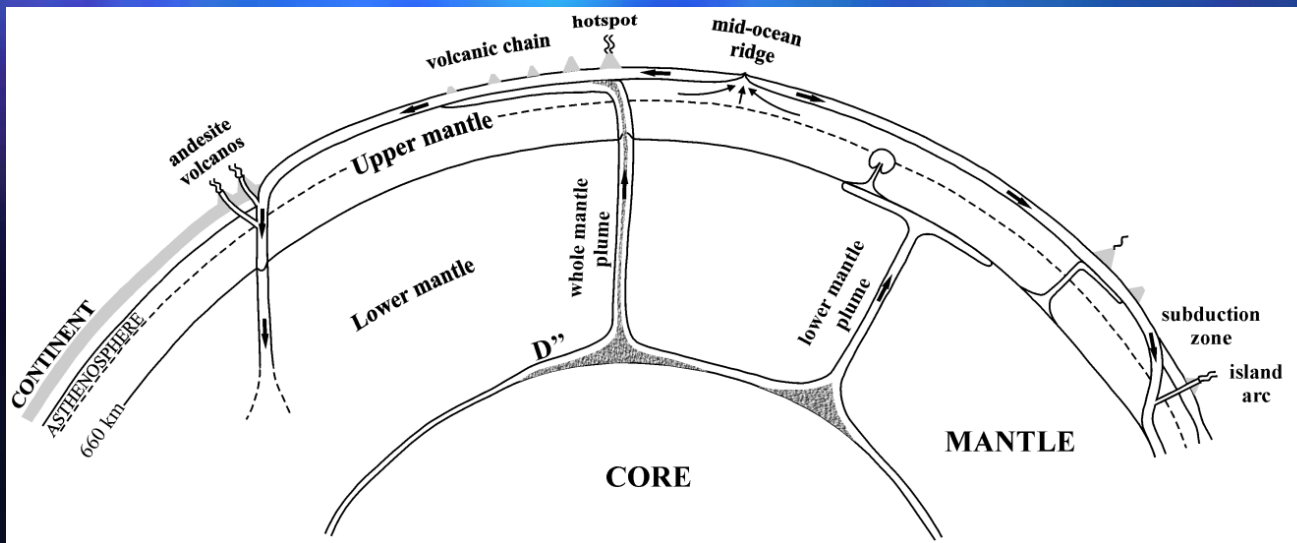
Thermal convection in a tank and in the Earth's mantle



# Thermo-chemical convection (TCC)



Seismic tomography of the mantle,  
blue - fast, red – slow  
[Tackley 2000].



Conceptual model on the  
thermo-chemical convection  
in the Earth's mantle  
[Galsa et al. 2008].

# Comsol model

## Chemical density difference:

$\beta=0.1\% - 2\%$ , relative density difference between D'' and the overlaying mantle

## Buoyancy ratio:

$$B = \frac{\text{'chemical density difference'}}{\text{'thermal density difference'}} = \frac{\beta}{\alpha \cdot \Delta T}$$

**Finite elements:** 73772 (triangle advancing front)

**Size:** outer radius 6370 km  
inner radius 3470 km

**Subdomains:** 2 (D'', overlaying mantle)

**Thickness of D'':** 300 km (flchs, 50 km)

**Artificial diffusion:** streamline, crosswind, isotropic

## Boussinesq approximation:

Conservation of mass

$$\frac{\partial u_i}{\partial x_i} = 0$$

Conservation of momentum

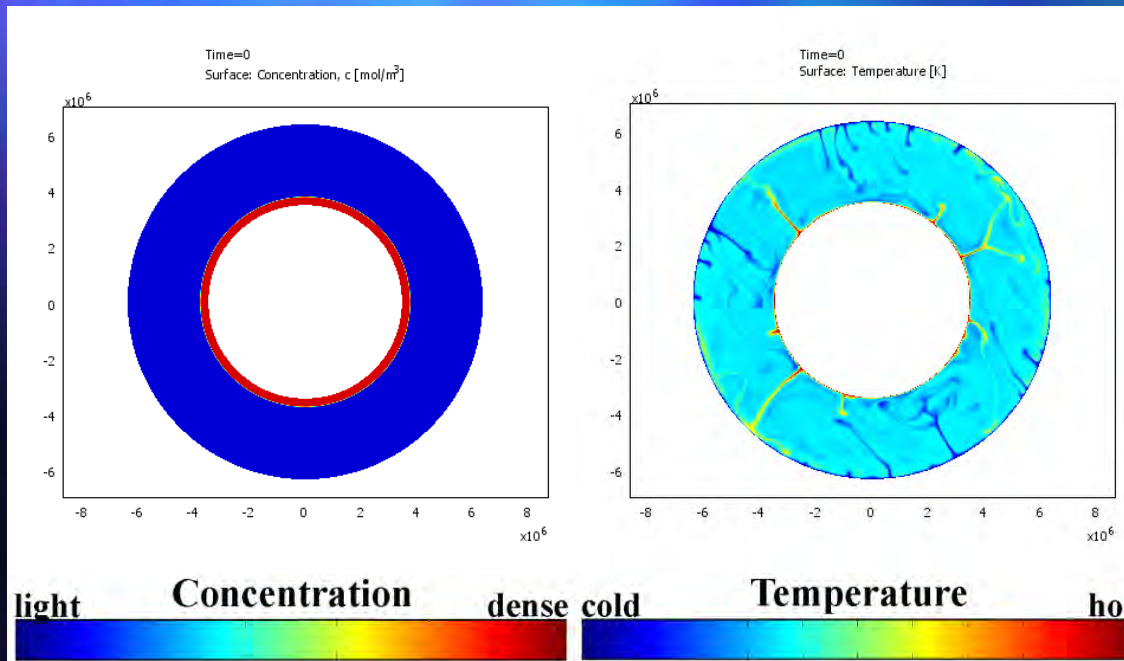
$$\rho \frac{du_i}{dt} = \rho g e_i - \frac{\partial p}{\partial x_i} + \frac{\partial \sigma_{ij}}{\partial x_j}$$

Heat transport

$$\frac{\partial T}{\partial t} = \kappa \frac{\partial^2 T}{\partial x_i^2} - u_i \frac{\partial T}{\partial x_i}$$

Mass transport

$$\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial x_i^2} - u_i \frac{\partial c}{\partial x_i}$$

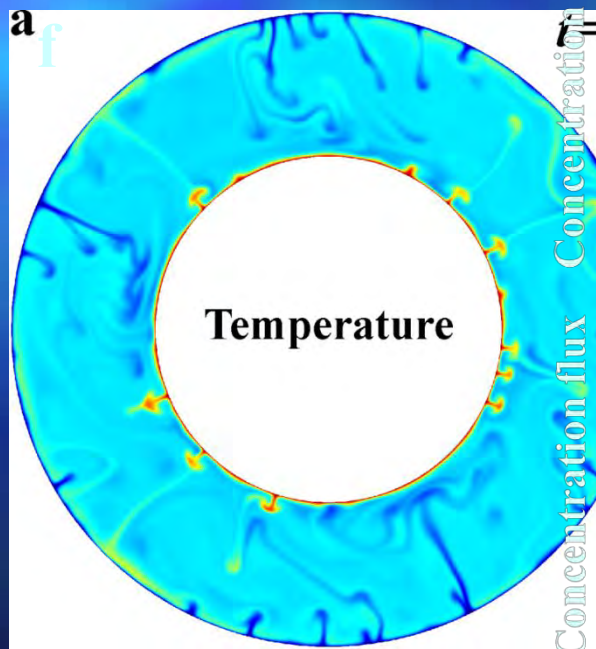
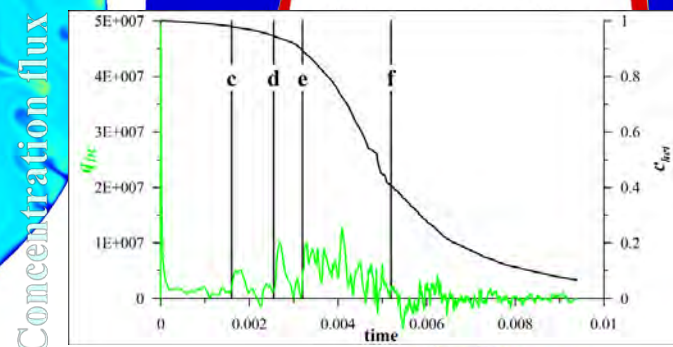
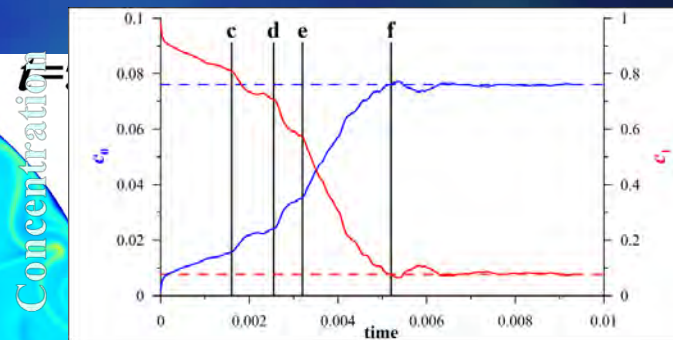
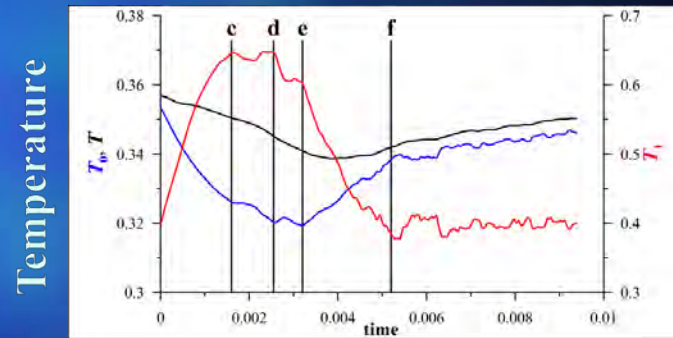
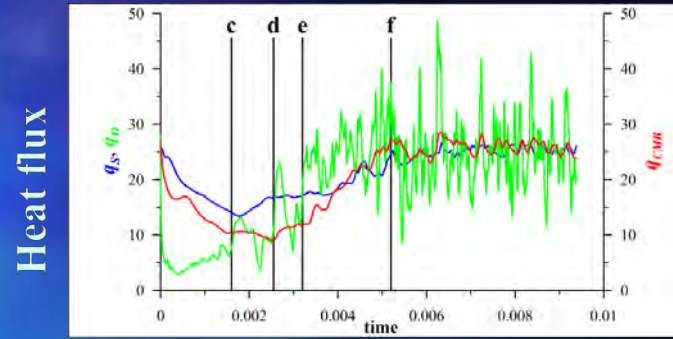


**Thermo-chemical mantle convection at  $\beta=1\%$  relative density contrast between the D'' and the overlaying mantle.**

# Results

## Seven stages of TCC

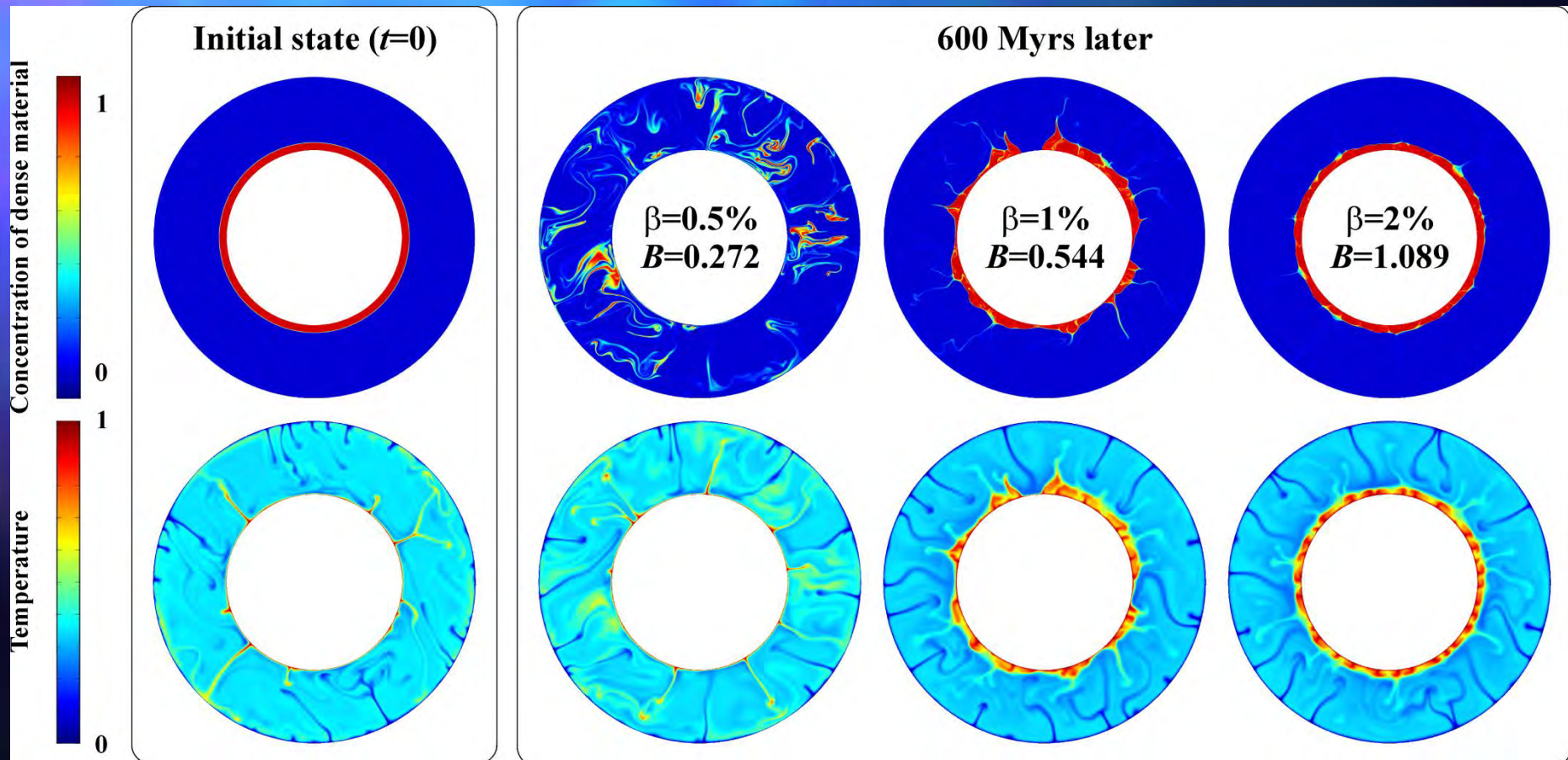
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- $\beta=1\%$
- a. deformation of D'' layer
- b. developed two-layer thermal convection
- c. disintegration of D''
- d. onset of one-layer TCC
- e. first dome ceased
- f. last dome ceased / mixed mantle
- g. homogeneous mantle

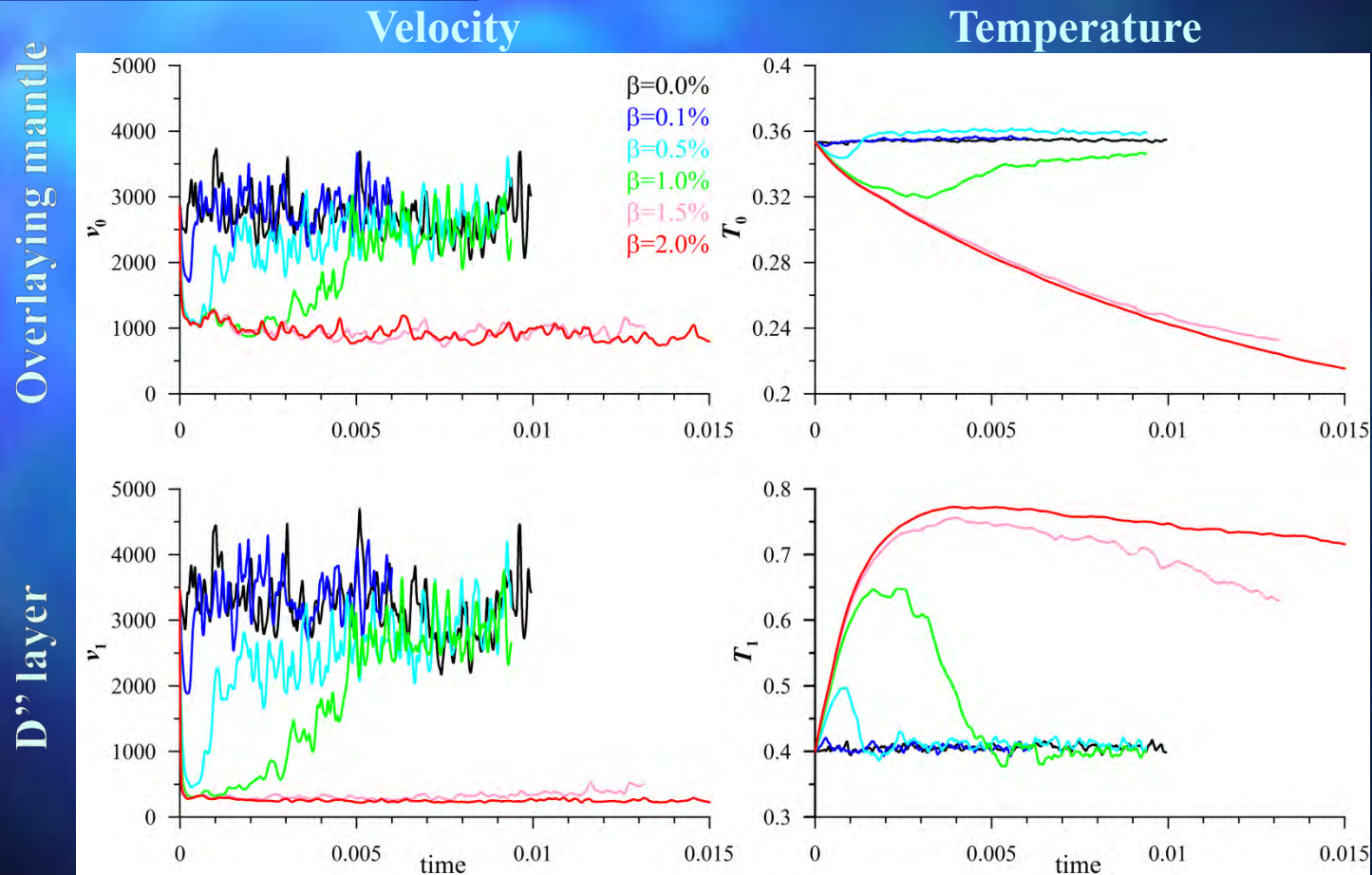


## Effect of density difference ( $\beta$ )



The concentration of the dense material and the temperature at the initial state ( $t=0$ ) and 600 Myrs later at different density contrasts ( $\beta$ ).

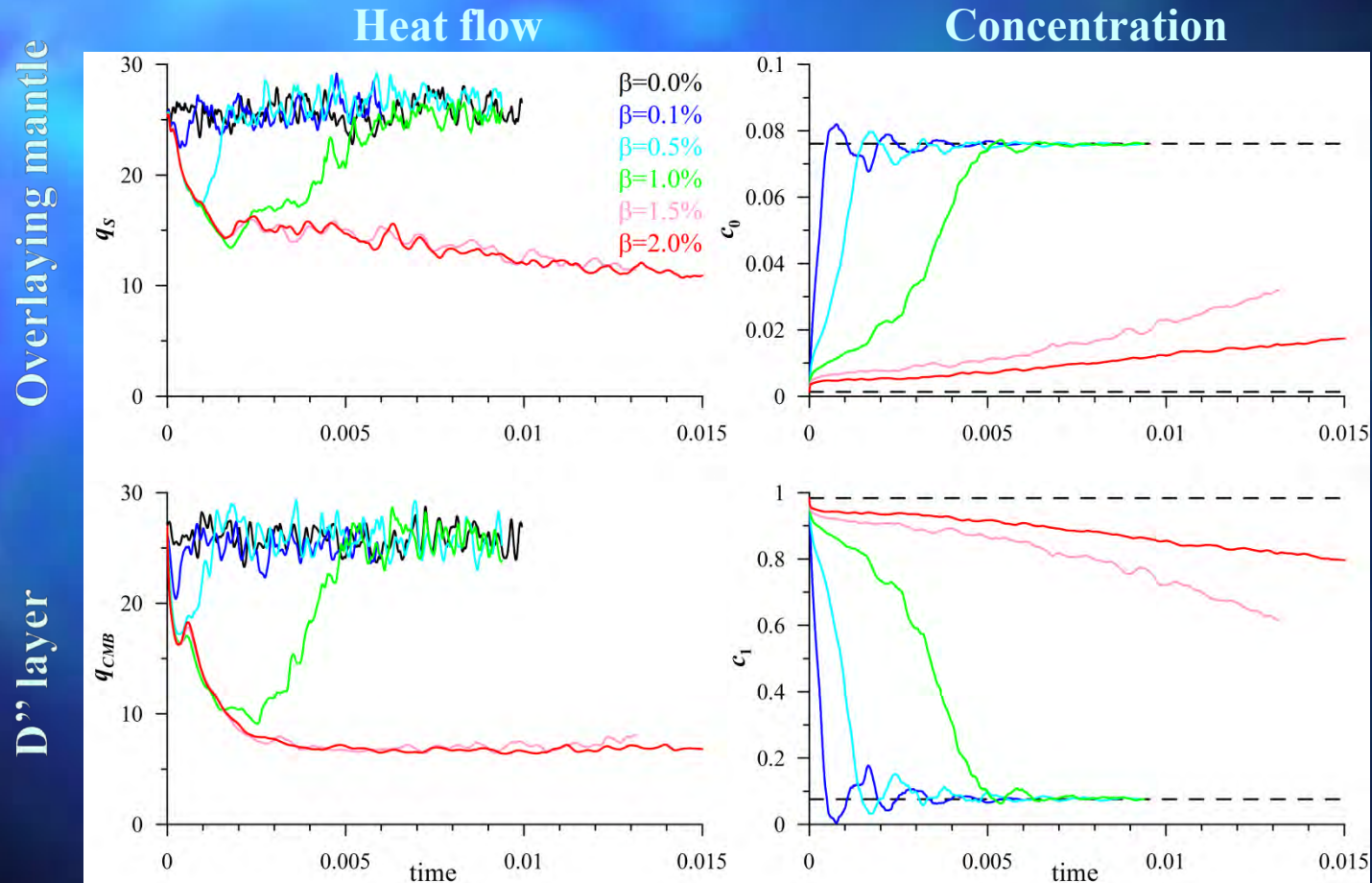
# Effect of density difference ( $\beta$ ) – Time series I



Velocity and temperature time series in the D'' layer and the overlaying mantle at different density contrasts ( $\beta$ ).



# Effect of density difference ( $\beta$ ) – Time series II



Heat flow and concentration time series in the D'' layer and the overlaying mantle at different density contrasts ( $\beta$ ).

## Time-dependent Buoyancy ratio

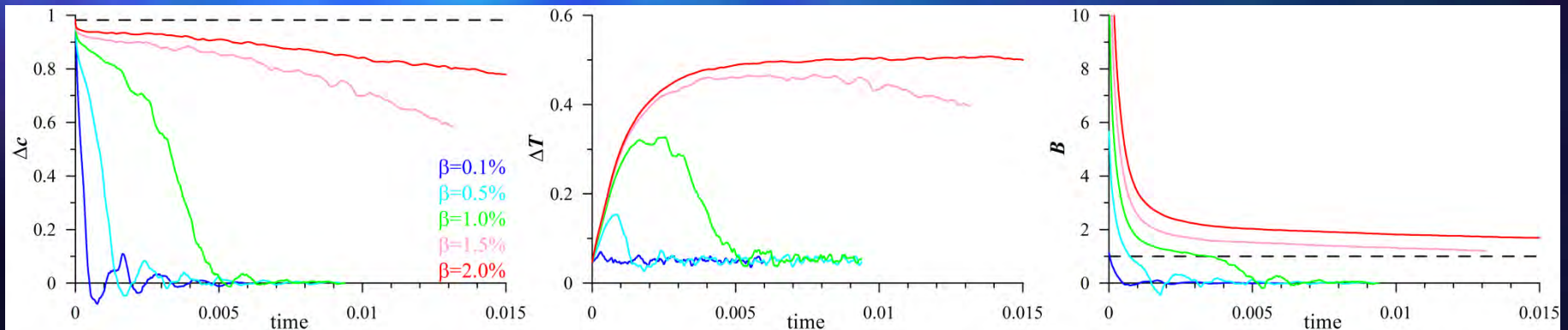
$$B = \frac{\text{'chemical density difference'}}{\text{'thermal density difference'}} = \frac{\beta}{\alpha \cdot \Delta T}$$



Traditional definition

$$B(t) = \frac{\text{'chemical density difference'}}{\text{'thermal density difference'}} = \frac{\beta \cdot \Delta c(t)}{\alpha \cdot \Delta T(t)} = \frac{\beta \cdot (c_1 - c_0)}{\alpha \cdot (T_1 - T_0)}$$

Reinterpreted definition



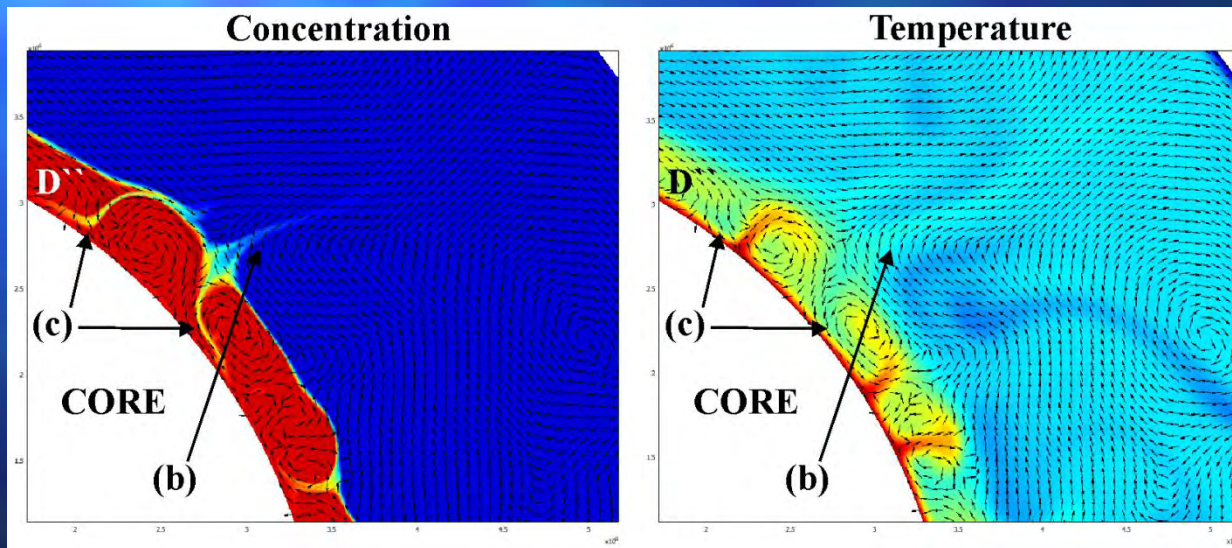
Time-dependent concentration and temperature difference between D'' and the upper layer as well as the calculated Buoyancy ratio at different density contrasts ( $\beta$ ).

## Processes decreasing $B$

$$B = \frac{\beta \cdot \Delta c(t)}{\alpha \cdot \Delta T(t)}$$

Three main processes decrease  $B$  in time:

- a heat coming from the core warms up the dense layer reducing its density by thermal expansion;
- b thermal convection evolving in the upper layer erodes the surface of the dense layer;
- c thermal convection forming in the D'' layer intermixes the light material from the overlaying zone.



Two processes decreasing the concentration difference between D'' and the overlaying mantle.



# Conclusions

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- Existence of the dense D'' layer around the core influences considerably the time-dependent parameters (heat flux, velocity, temperature, concentration) characterizing the flow regime.
- Good correlation was found between the evolution of D'' layer and the time-series of the parameters monitored during the simulation.
- New interpretation of the buoyancy ratio was offered to help the understanding of the thermo-chemical processes in the mantle.

**Thank you for the  
attention!**