

Computational Building Physics

using COMSOL

Research, Education & Practice

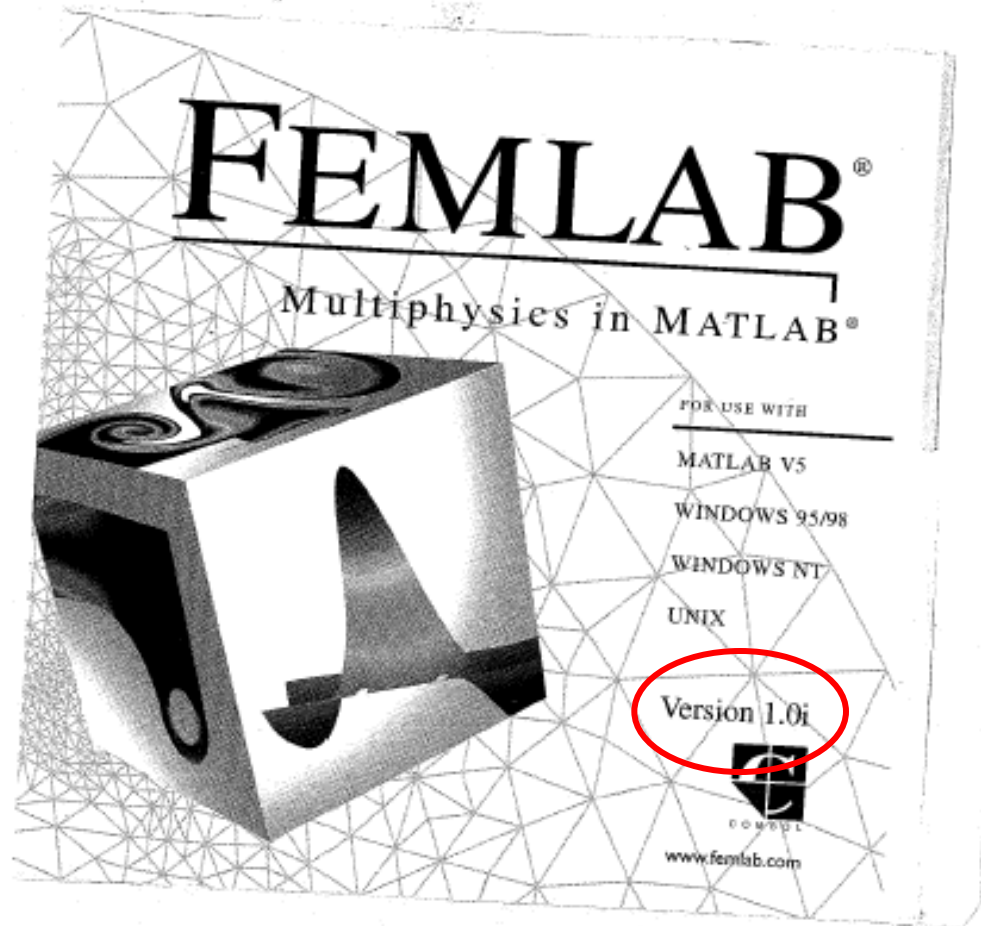
dr.ir. Jos van Schijndel

TU / **e**

Technische Universiteit
Eindhoven
University of Technology

Where innovation starts

User since 1998(?)



Contents

- **1. Introduction**
 - Complexity and scale levels
 - My computational laboratory
- **2. Combined heat, moisture, air, stress models for (building) constructions**
- **3. From Material [\sim mm] to EU [\sim Mm] scale level**
- **4. Conclusions**

1. Introduction

Complexity and Scale levels

- What is a 'Complex system'?
- Where are Complex systems in the built environment?

Introduction

Complexity and Scale levels

- The whole is greater than the sum of the individual parts



Introduction

Complexity and Scale levels

- **Butterfly effect: Small parameter variations may produce large variations in the long term behavior of the system.**



Introduction

Complexity and Scale levels

- Where are the dynamic complex systems at the built environment ?

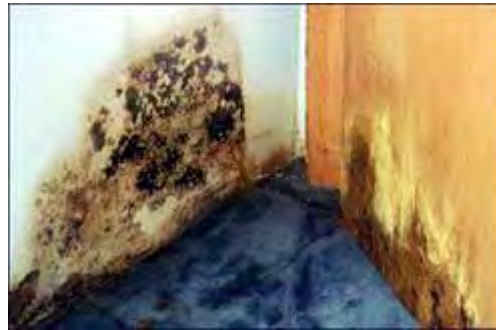
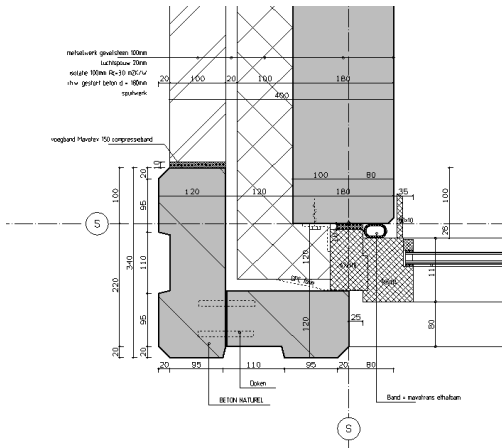
Everywhere and on several scales



Scale levels, from left to right: EU; Urban area; Building; Material;

Introduction

Complexity and Scale levels



Material ~ mm

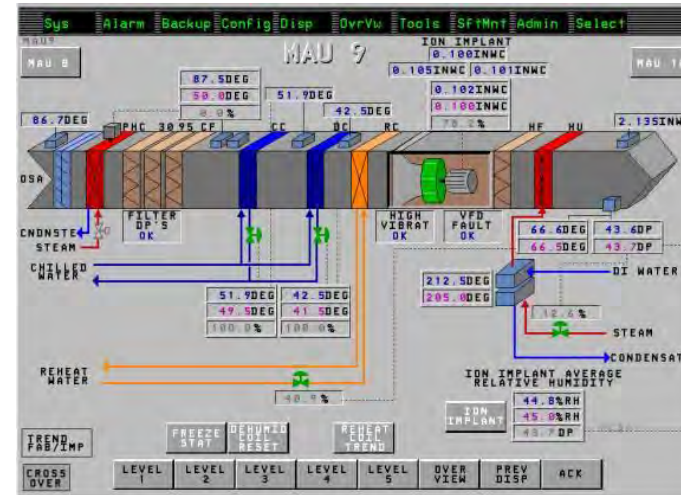
Present dynamic complex systems:

Material Physics

- Durability

Introduction

Complexity and Scale levels



Building ~ 10 m

Present dynamic complex systems:

Building Physics

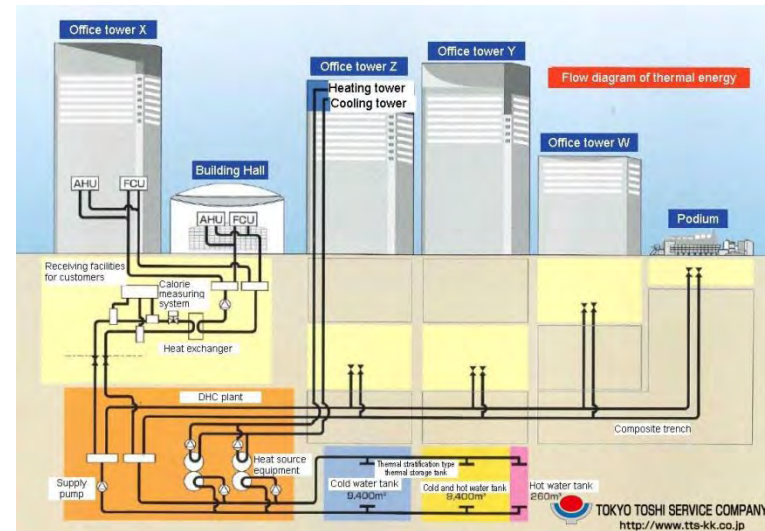
- Indoor climate
- Building systems

Introduction

Complexity and Scale levels



Urban Area ~ km



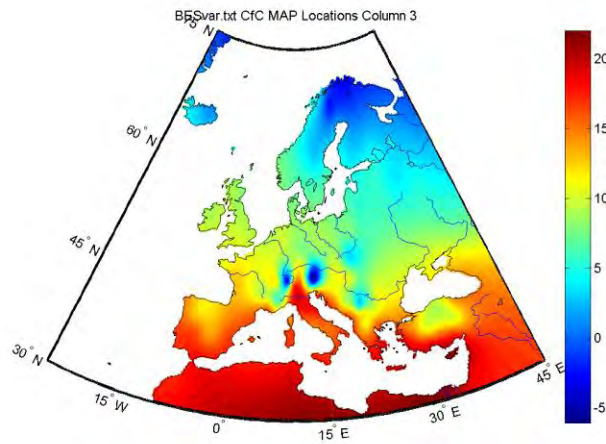
Present dynamic complex systems:

Urban Physics

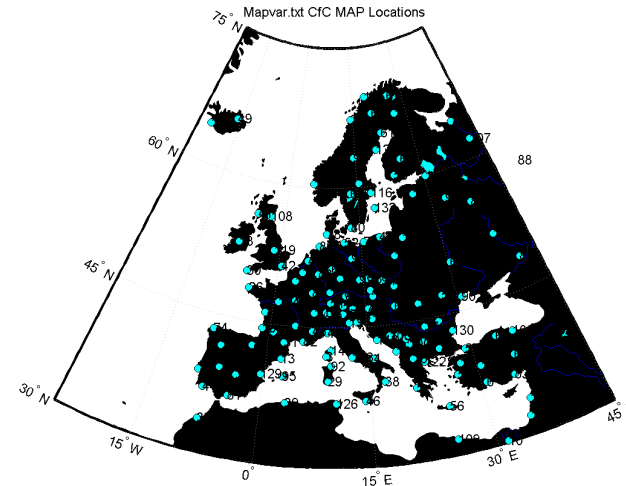
- Urban Climate
- Urban district systems

Introduction

Complexity and Scale levels



EU ~ 1 Mm



- Present dynamic complex systems:
- Global climate Physics
 - (Future) Climate
 - Mapping

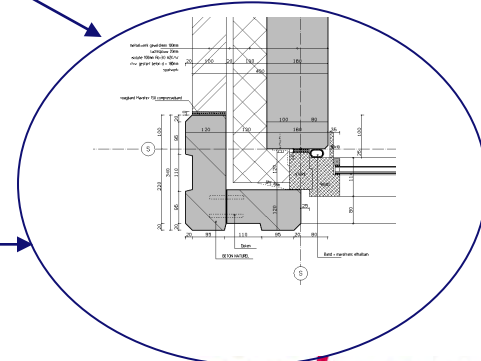
Introduction

My computational laboratory

Multi Buildings
'HAMBase'
MatLab



Multi Details
PDE
Comsol

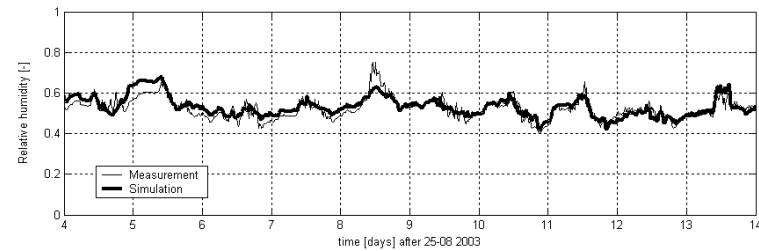
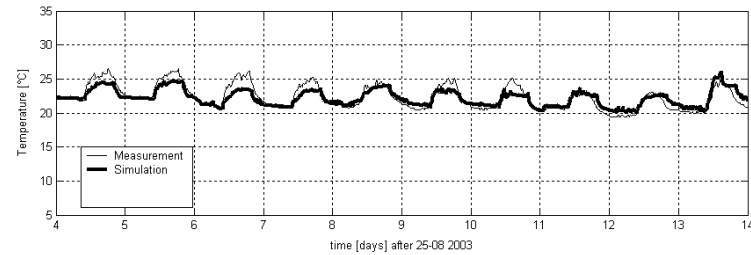


Multi Systems & Control
ODE
SimuLink



Tools Buildings modeling physics: **HAMBase** scientific software: **MatLab**

Simulation and validation

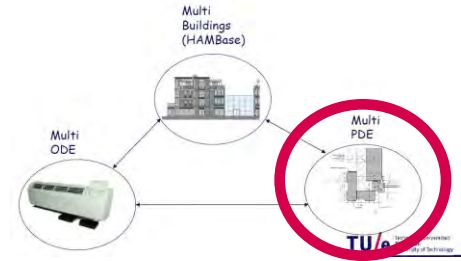


Anne Frank House



Tools Detail modeling

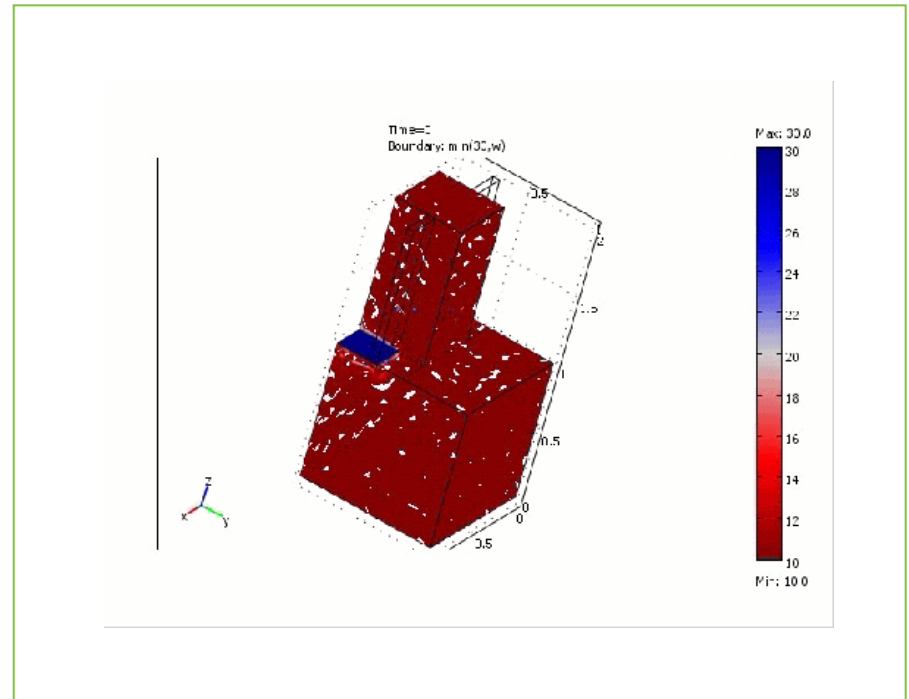
physics: **PDEs**
scientific software: **Comsol**



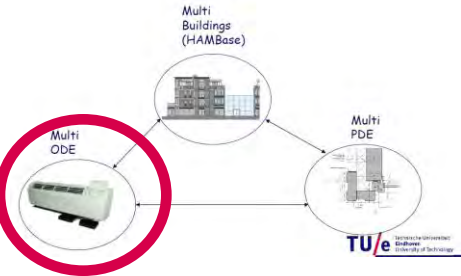
Hunting Logde St. Hubertus



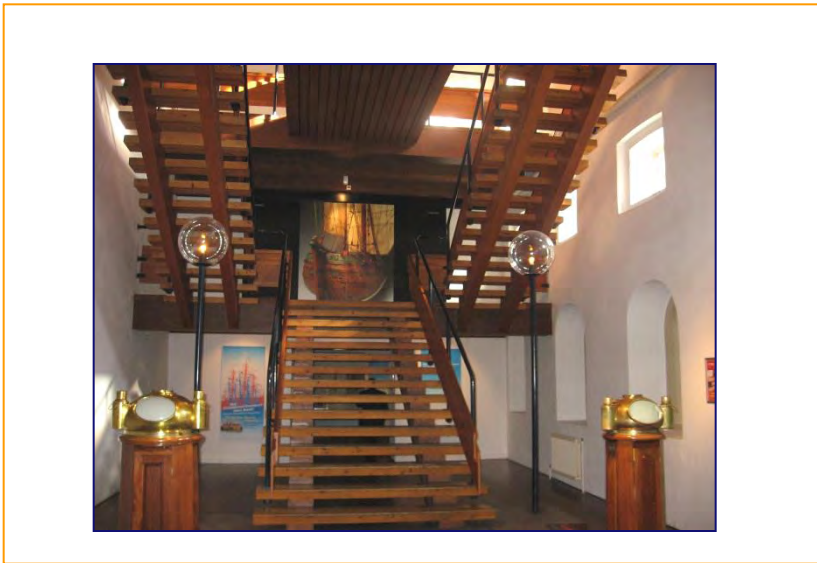
3D Moisture



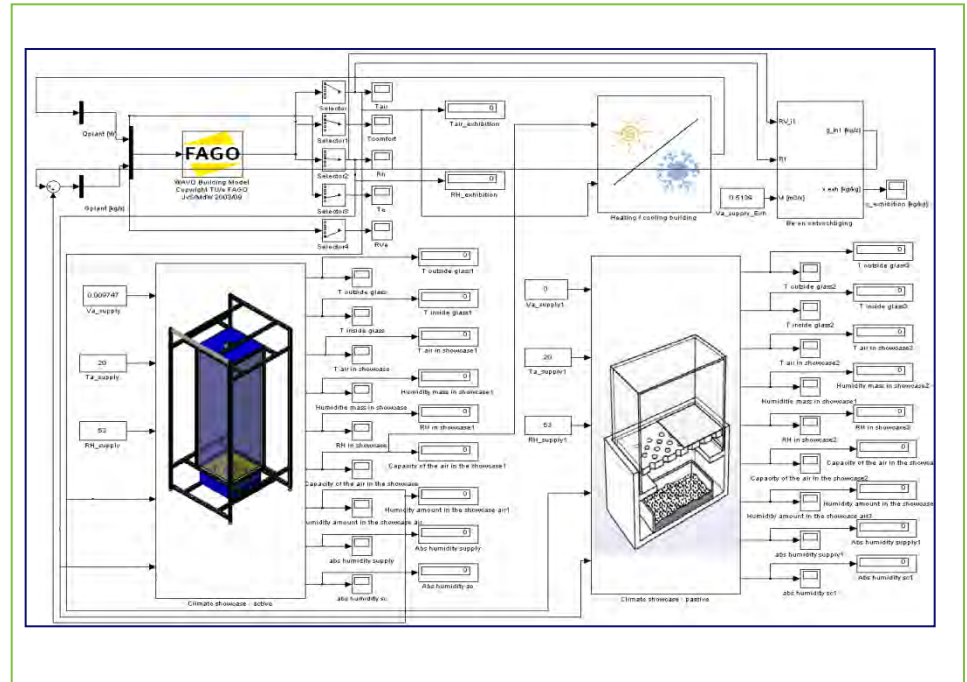
Tools Systems&Control modeling physics: ODEs scientific software: SimuLink



Dutch Maritime Museum

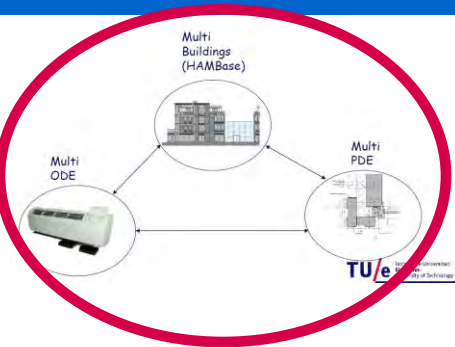


Building systems failure modeling

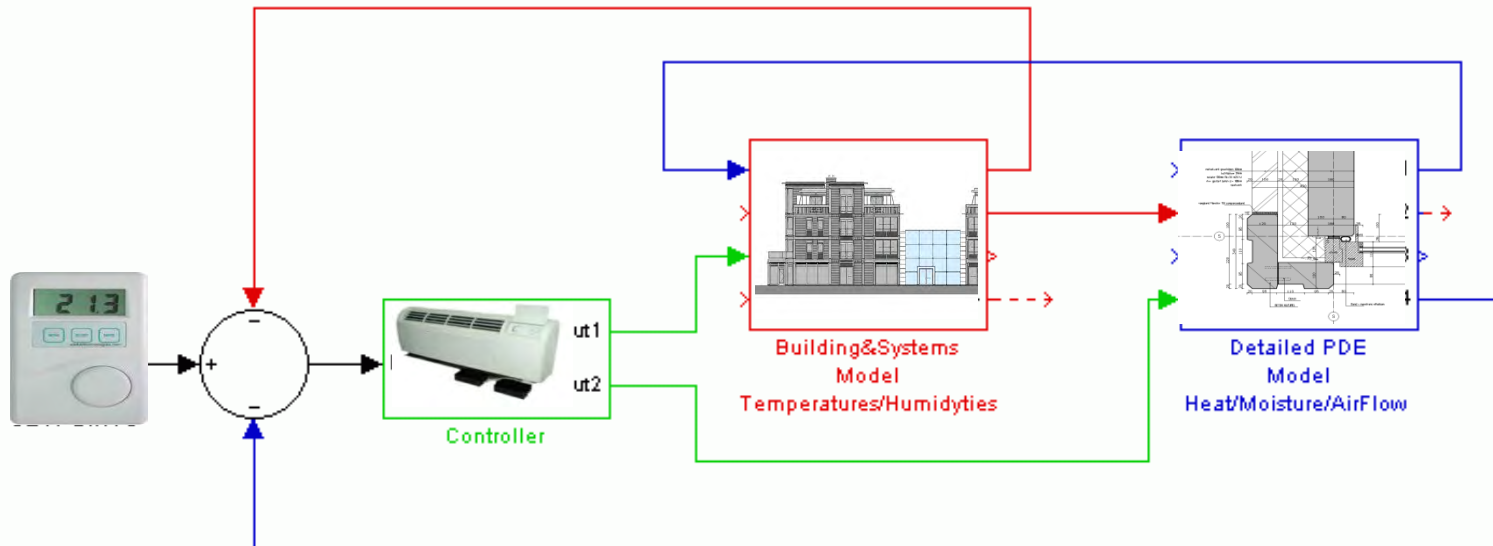


Introduction

My computational laboratory

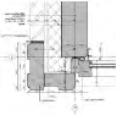


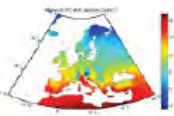


<http://archbps1.campus.tue.nl/bpswiki/index.php/Hamlab>



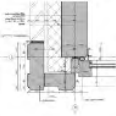


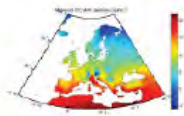
Computational Building Physics

Research Matrix

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

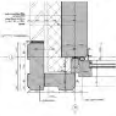


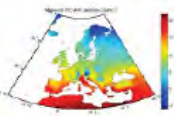
Computational Building Physics

Heat

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

Computational Building Physics

Heat+Moisture

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

Application 2: Heat and moisture transport PDEs

- Potential T, LPc
- PDE coefficients formulation
 - Material properties
 - function of T, LPc

$$C_T \frac{\partial T}{\partial t} = \nabla \cdot (K_{11} \nabla T + K_{12} \nabla LPc)$$

$$C_{LPc} \frac{\partial LPc}{\partial t} = \nabla \cdot (K_{21} \nabla T + K_{22} \nabla LPc)$$

$$LPc = {}^{10} \log(Pc)$$

$$C_T = \rho \cdot c$$

$$K_{11} = \lambda$$

$$K_{12} = -l_{iv} \cdot \delta_p \cdot \phi \cdot \frac{\partial Pc}{\partial LPc} \cdot P_{sat} \cdot \frac{M_w}{\rho_a RT},$$

$$C_{LPc} = \frac{\partial w}{\partial Pc} \cdot \frac{\partial Pc}{\partial LPc}$$

$$K_{22} = -K \cdot \frac{\partial Pc}{\partial LPc} - \delta_p \cdot \phi \cdot \frac{\partial Pc}{\partial LPc} \cdot P_{sat} \cdot \frac{M_w}{\rho_a RT},$$

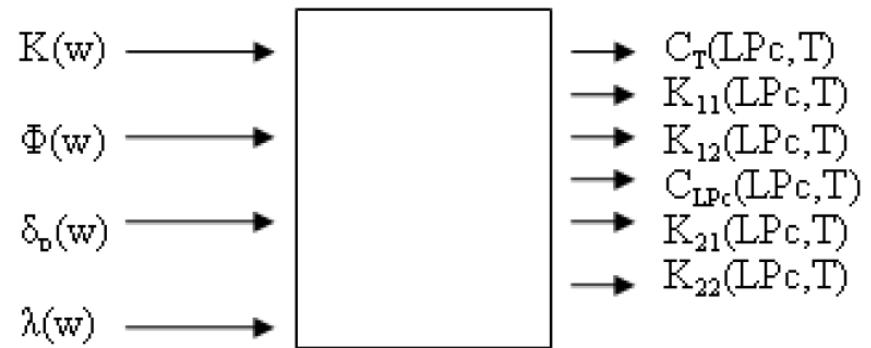
$$K_{21} = \delta_p \cdot \phi \cdot \frac{\partial P_{sat}}{\partial T},$$

Calculating PDE coefficients using material properties, method 1/2

- **PDE coefficients lookup tables calculated in MatLab using:**
 - **heat conduction coefficients**
 - **specific heat**
 - **density**
 - **liquid permeability**
 - **moisture retention curve**
 - **vapour permeability**

$$C_T \frac{\partial T}{\partial t} = \nabla \cdot (K_{11} \nabla T + K_{12} \nabla LPc)$$

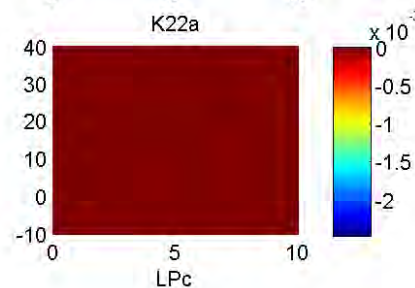
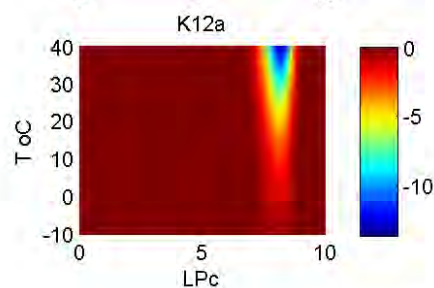
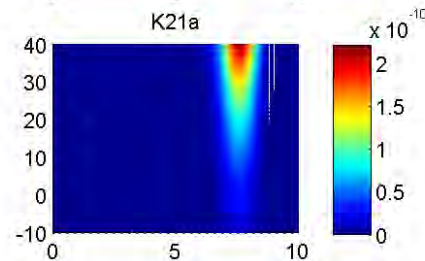
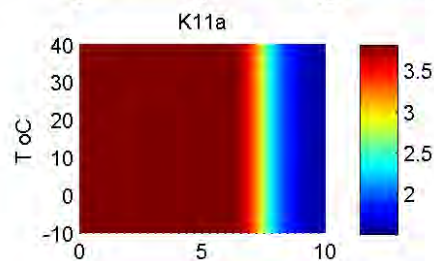
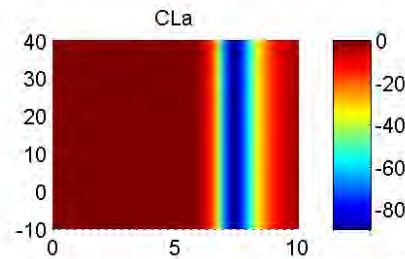
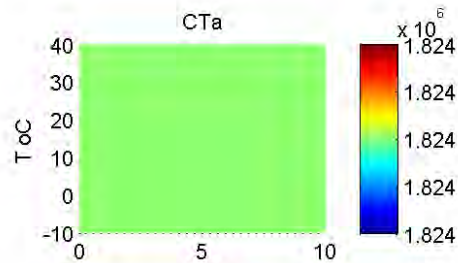
$$C_{LPc} \frac{\partial LPc}{\partial t} = \nabla \cdot (K_{21} \nabla T + K_{22} \nabla LPc)$$



Calculating PDE coefficients using material properties, result 2/2

$$C_T \frac{\partial T}{\partial t} = \nabla \cdot (K_{11} \nabla T + K_{12} \nabla LPc)$$

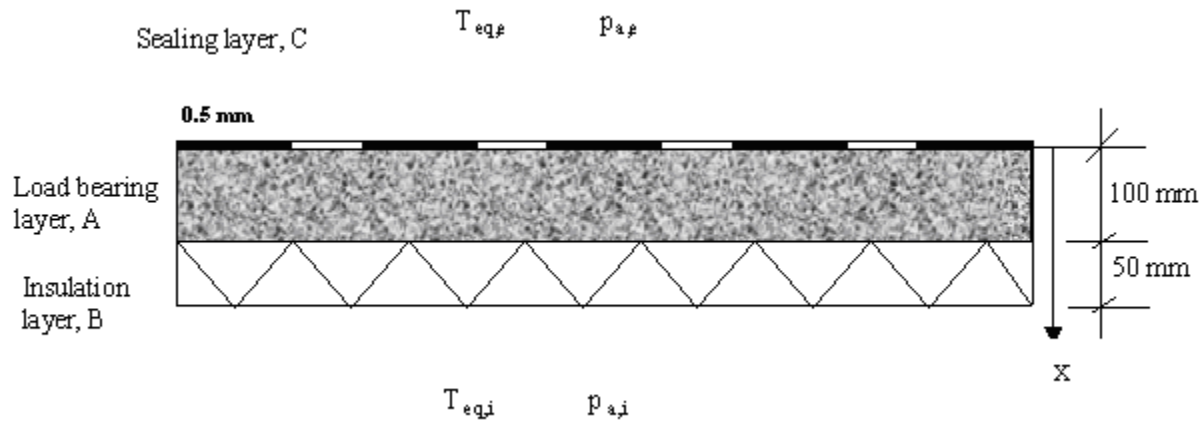
$$C_{LPc} \frac{\partial LPc}{\partial t} = \nabla \cdot (K_{21} \nabla T + K_{22} \nabla LPc)$$



Verification HAMSTAD Benchmark no 1

$$q = h_e \cdot (T_e - T)$$

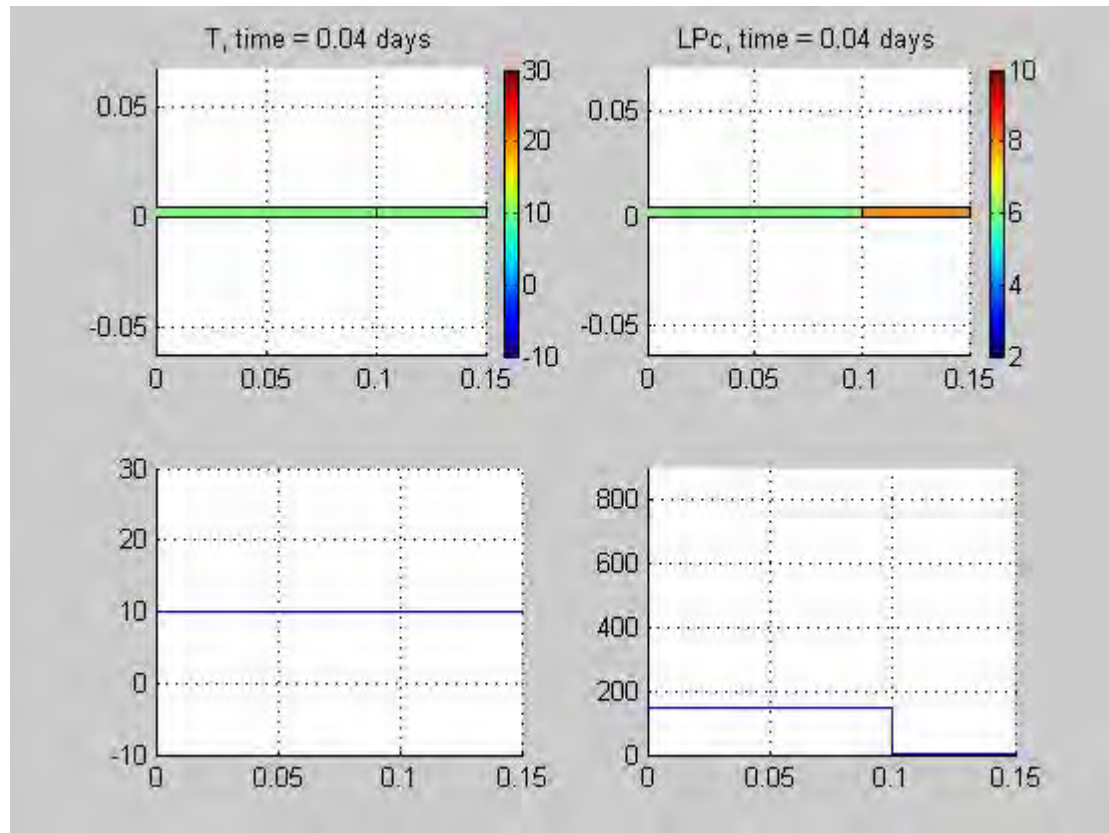
$$g = 0$$



$$q = h_i \cdot (T_i - T) + l_{lv} \cdot \beta \cdot (p_i - p)$$

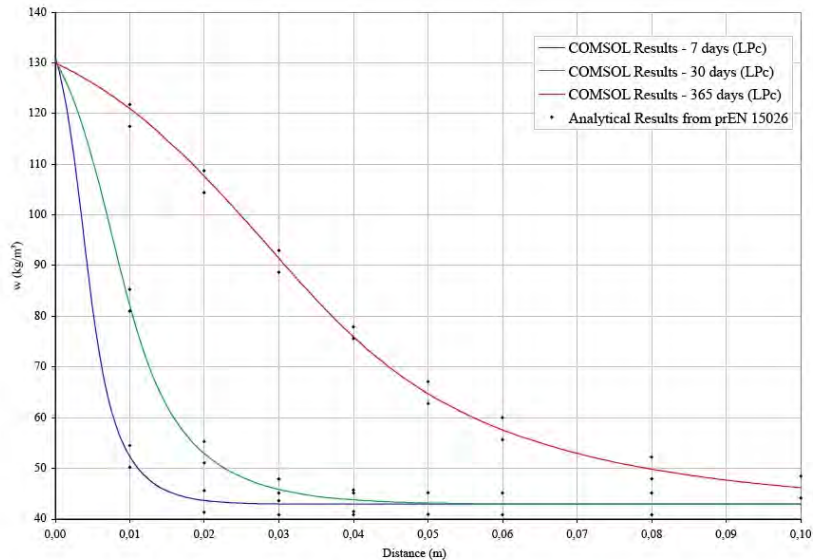
$$g = \beta \cdot (p_i - p)$$

Verification Heat & Moisture

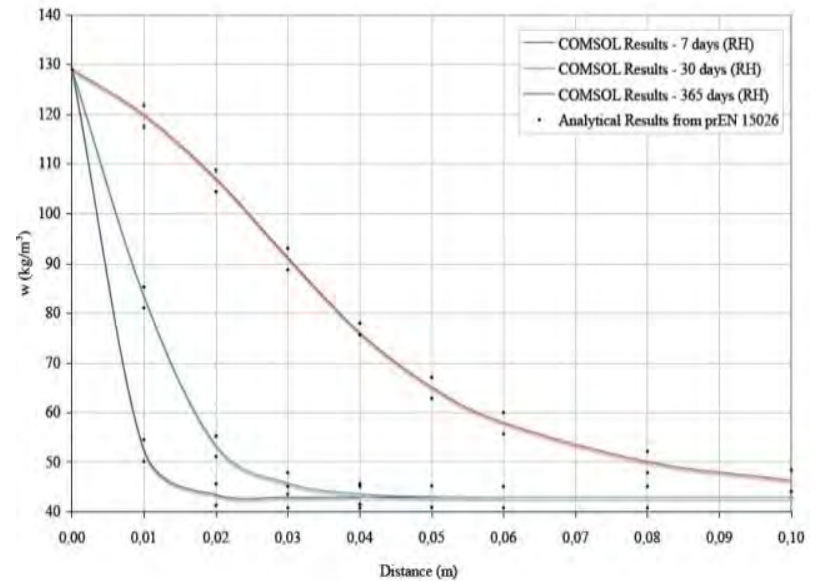


Verification Moisture

LPc based model

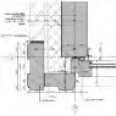


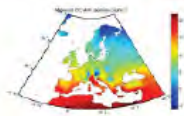


RH based model



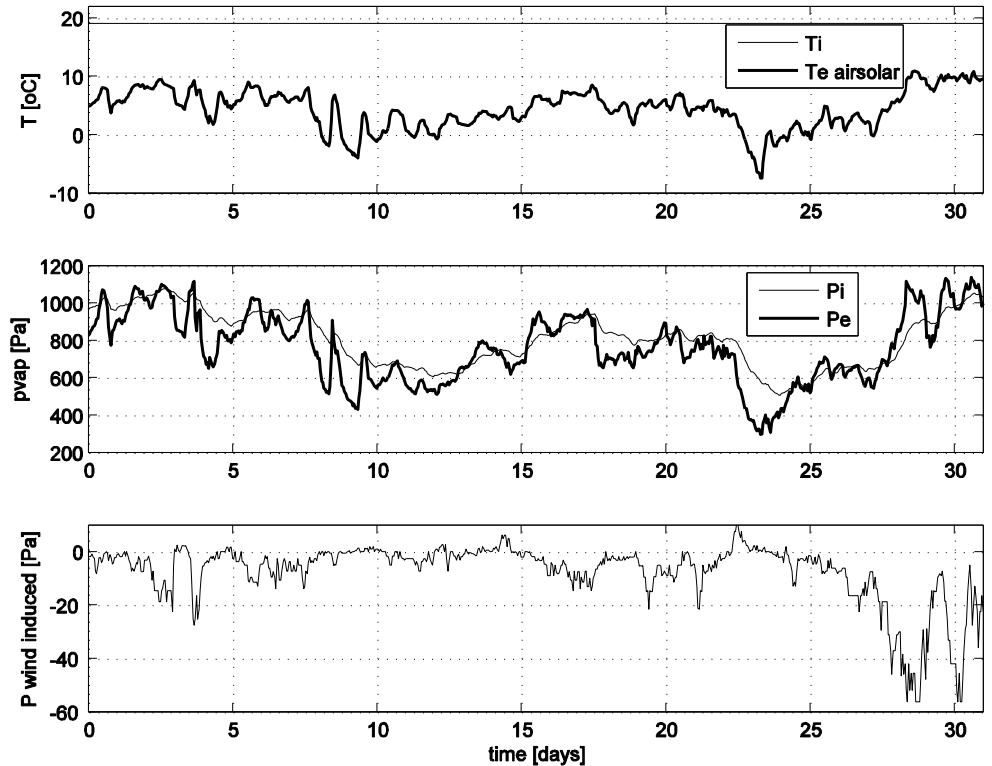
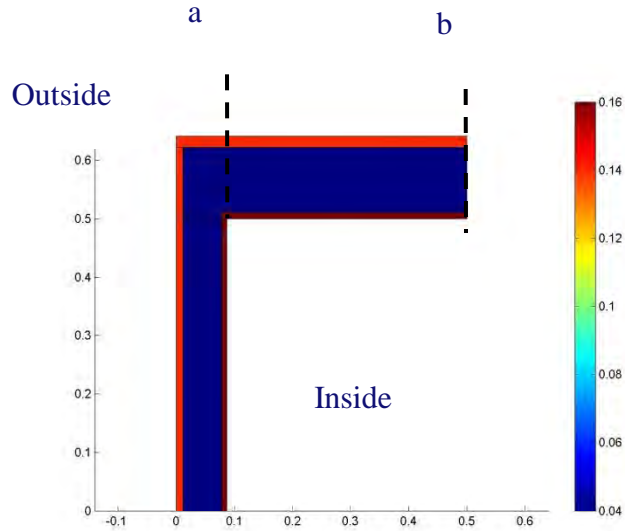
Computational Building Physics

Heat+Moisture+Air

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

Application 3 HAM modeling

Influence of micro air movement



HAM modeling Physics

PDEs

$$\text{Heat} : \rho C_p \frac{\partial T}{\partial t} + \nabla \cdot (-\lambda \nabla T) + \rho C_p \mathbf{u} \cdot \nabla T = 0$$

$$\text{Air} : \frac{\partial P}{\partial t} + \nabla \cdot (-K \nabla P) = 0; \mathbf{u} = K \nabla P$$

$$\text{Moisture} : \frac{\partial p_v}{\partial t} + \nabla \cdot (-D \nabla p_v) + \mathbf{u} \cdot \nabla p_v = 0$$

Boundary values

$$\text{Heat} : \text{Flux} : \mathbf{n} \cdot (\lambda \nabla T) = h(T_{\text{inf}} - T); \text{Insulation} : \mathbf{n} \cdot (\lambda \nabla T) = 0$$

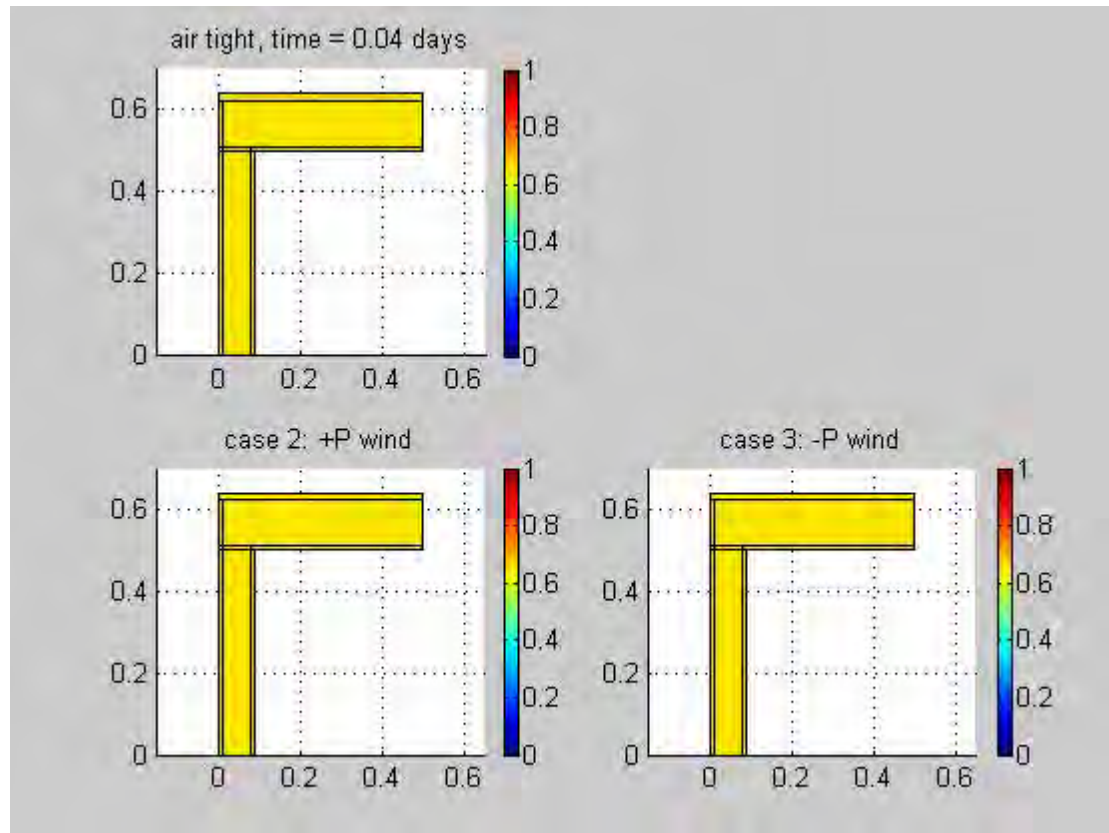
$$\text{Air} : \text{Pressure} : P = P_0; \text{Insulation} : \mathbf{n} \cdot K \nabla P = 0$$

$$\text{Moisture} : \text{Flux} : \mathbf{n} \cdot (D \nabla p_v) = \beta(p_{v\text{inf}} - p_v); \text{Insulation} : \mathbf{n} \cdot (D \nabla p_v) = 0$$

HAM modeling

Simulation of Relative Humidity

Air velocity
= 0

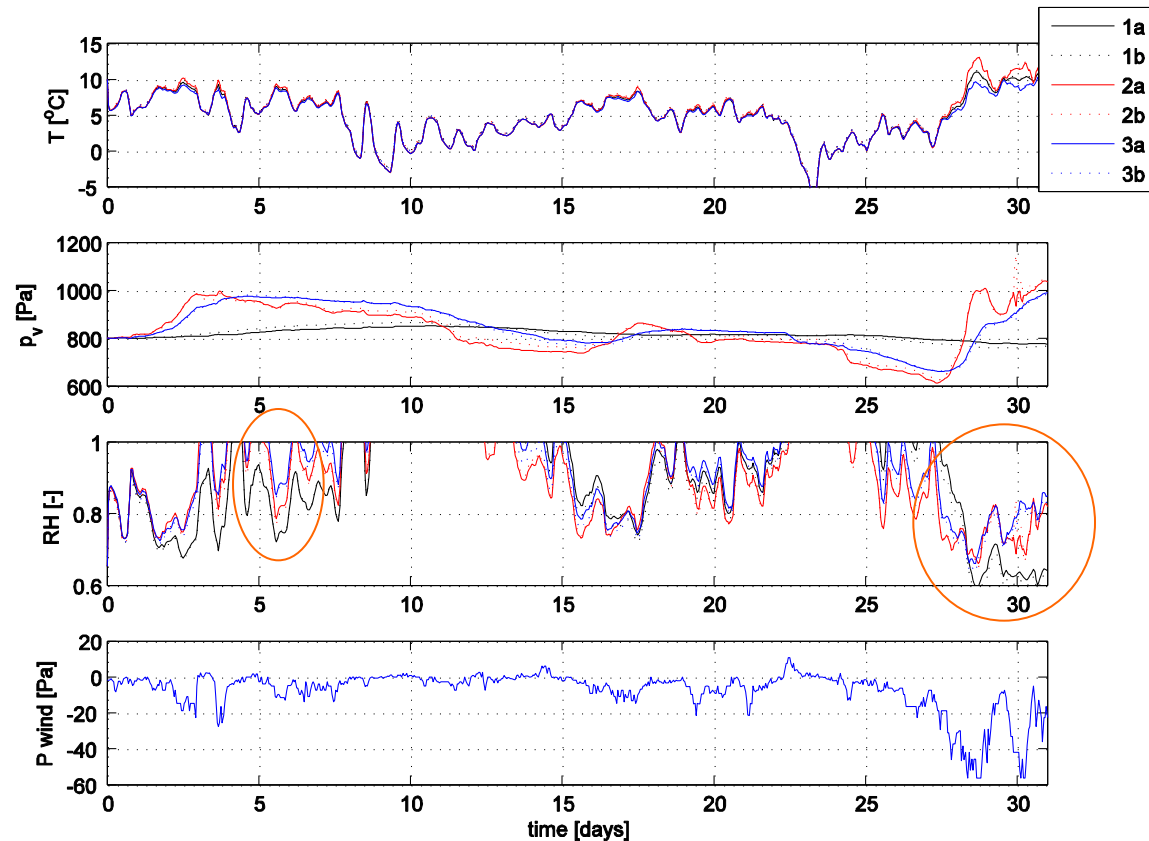
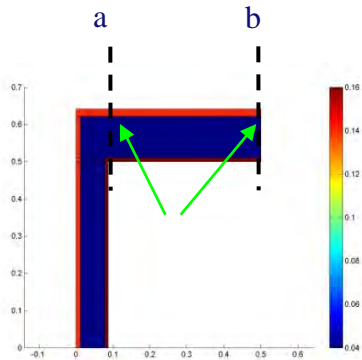


Air velocity
+10 $\mu\text{m} / \text{s}$

Air velocity
-10 $\mu\text{m} / \text{s}$

HAM modeling

Influence of micro air movement

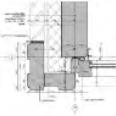


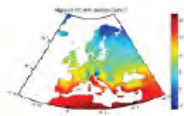


Summary

A (so far immeasurable) low air movement of order 10^{-5} m/s seems to have significant impact on the RH

Computational Building Physics

Heat+Moisture+Air+Stress

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

Application 4 HAMS modeling

Including stress and strain

$$\rho c_p \frac{\partial T}{\partial t} = \nabla(k \nabla T) \quad [1]$$

$$\frac{\partial P v}{\partial t} = \nabla(D(P v) \nabla P v) \quad [2]$$

$$\begin{pmatrix} \varepsilon_x \\ \varepsilon_y \\ \gamma_{xy} \end{pmatrix} = \begin{pmatrix} \frac{1}{E_x} & -\frac{\nu_{xy}}{E_y} & 0 \\ -\frac{\nu_{yx}}{E_x} & \frac{1}{E_y} & 0 \\ 0 & 0 & \frac{1}{G_{xy}} \end{pmatrix} \begin{pmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{pmatrix} + \begin{pmatrix} \alpha_x \\ \alpha_y \\ 0 \end{pmatrix} \Delta \theta + \begin{pmatrix} \kappa_x \\ \kappa_y \\ 0 \end{pmatrix} \Delta w \quad [5]$$

where:

$\varepsilon_x, \varepsilon_y$ = normal strain components [-]

γ_{xy} = shear strain component associated with two axis [-]

ν_{xy}, ν_{yx} = Poisson's ratio [-]

E_x, E_y = Young's moduli [N/m²]

G_{xy} = shear modulus [N/m²]

α_x, α_y = linear thermal expansivity [m/mK]

θ = temperature [°C]

κ_x, κ_y = linear deformation due to changes in moisture content [m/m(kg/m³)]

w = moisture content [kg/m³]

Application 4 HAMS modeling

Including stress and strain



Figure 2. Cracks in a door of one of the cabinets



Figure 1. Exploded view of the construction of one cabinet door (Source: Rijksmuseum, Amsterdam)

Application 4 HAMS modeling Including stress and strain

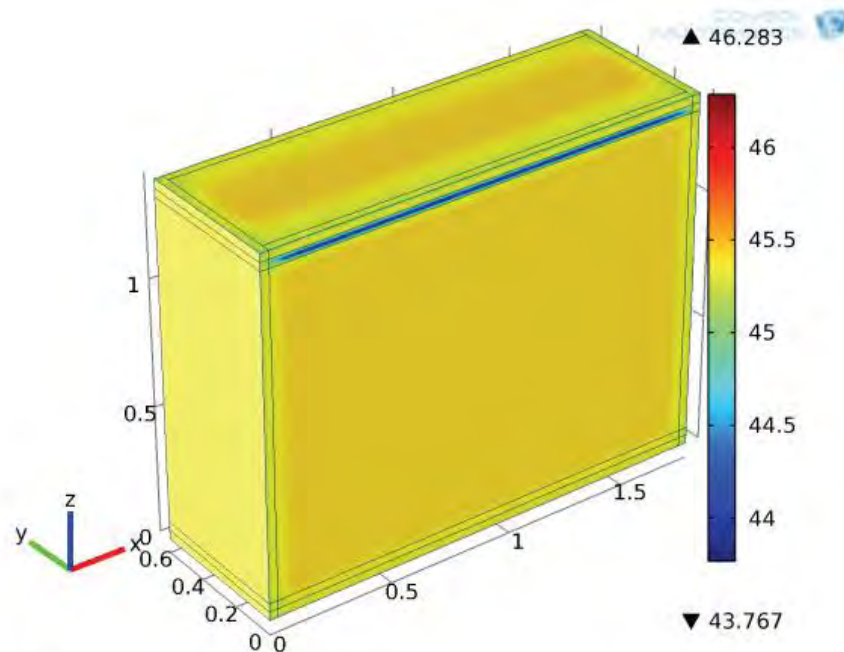


Figure 5. RH distribution over cabinet at $t = 1000$

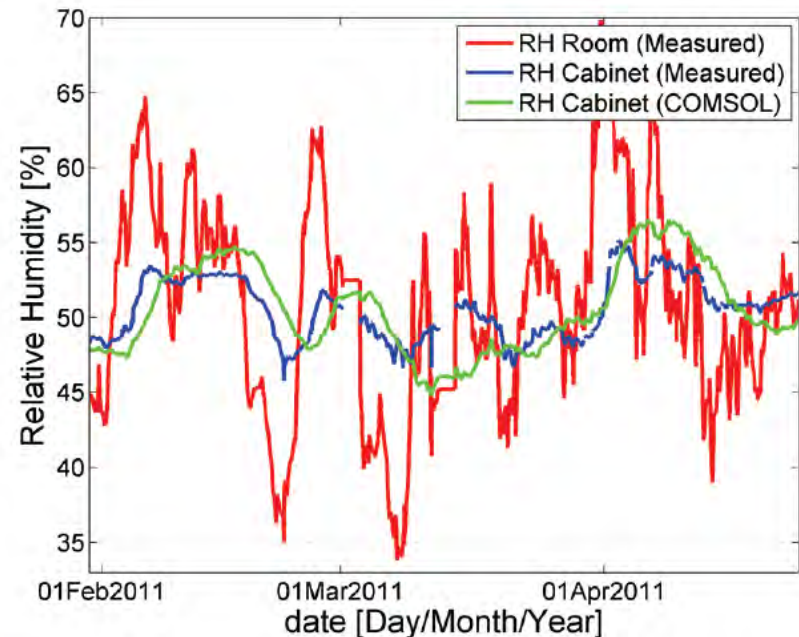


Figure 7. Comparison between measured relative humidity in castle and cabinet and simulated relative humidity in COMSOL

Application 4 HAMS modeling

Including stress and strain

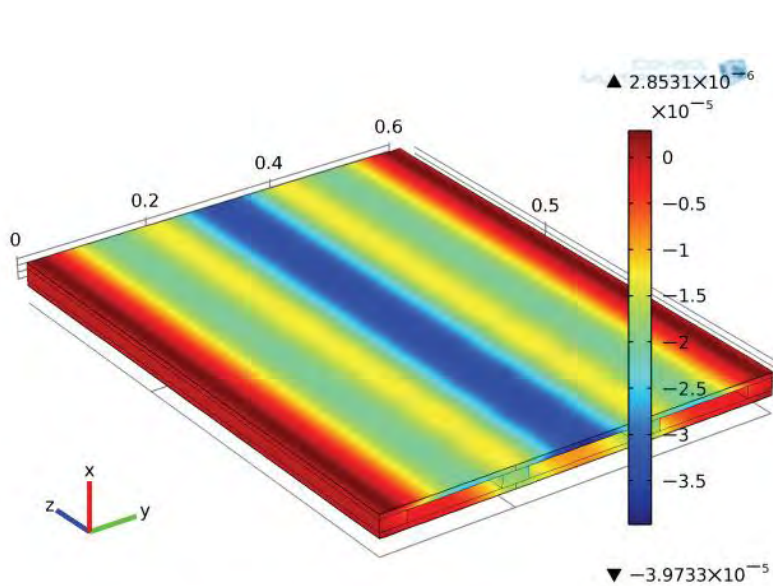


Figure 8. Predicted deformation at the external side of the cabinet door at $t = 1000$

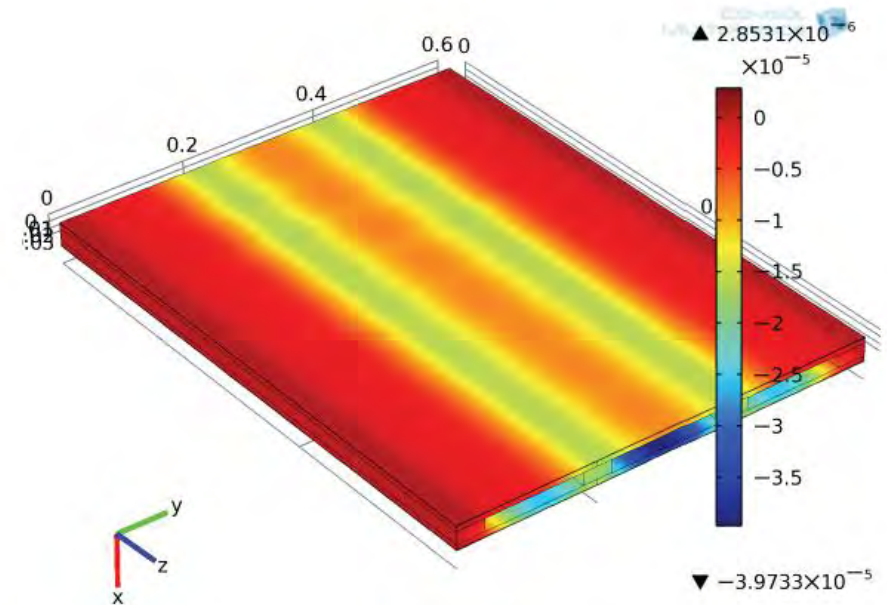
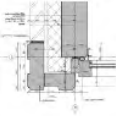


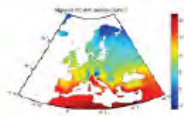


Figure 9. Predicted deformation at the internal side of the cabinet door at $t = 1000$

Thanks to: Zara Huijbregts (visit today, 4:00-5:30, Silchersaal)

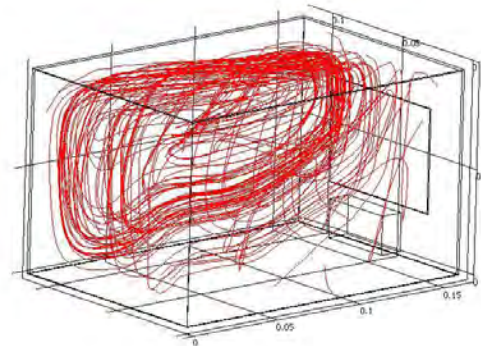
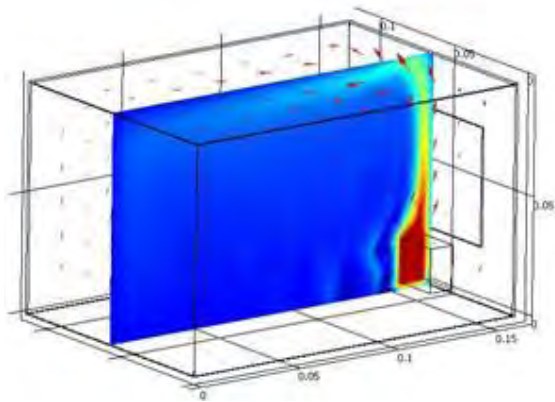
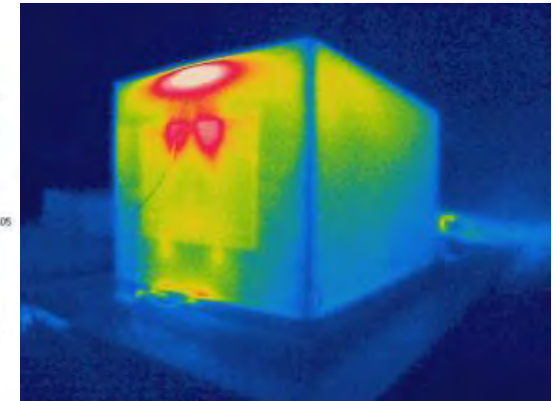
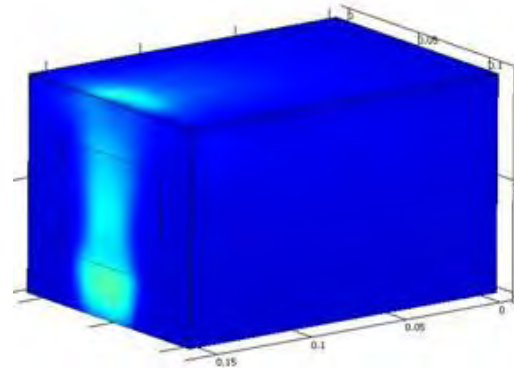
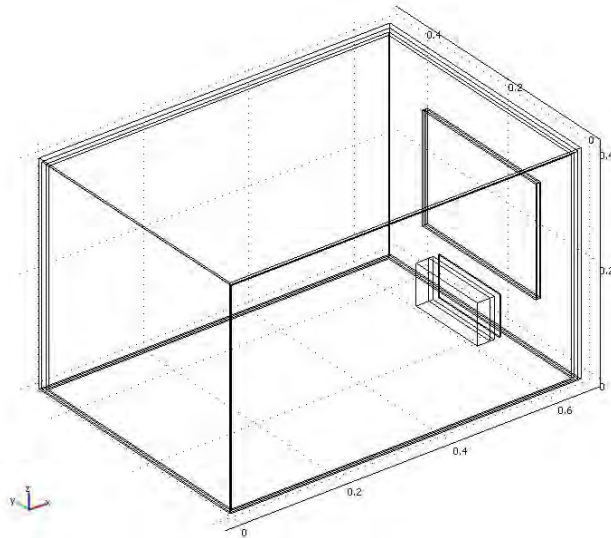
Computational Building Physics

Heat, including Building Scale

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

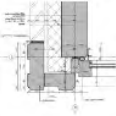


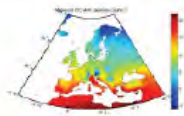
Application 5

Heat, including Building Scale



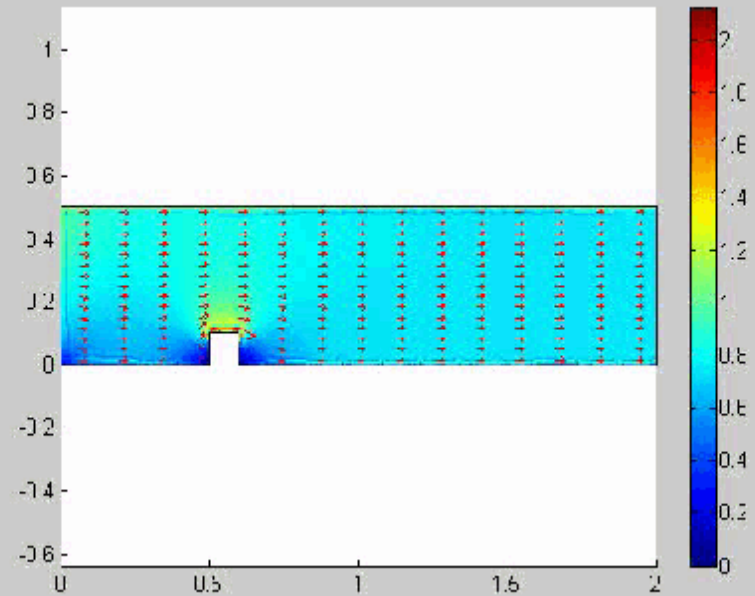
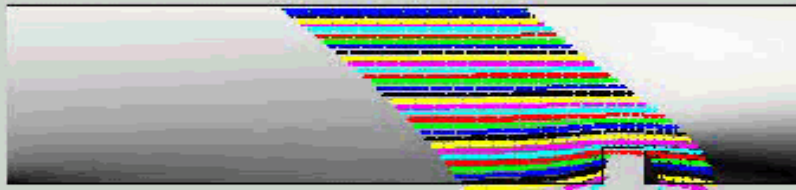
Computational Building Physics

Heat, including Urban Scale

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

Application 6

Wind & driving rain at Urban Scale

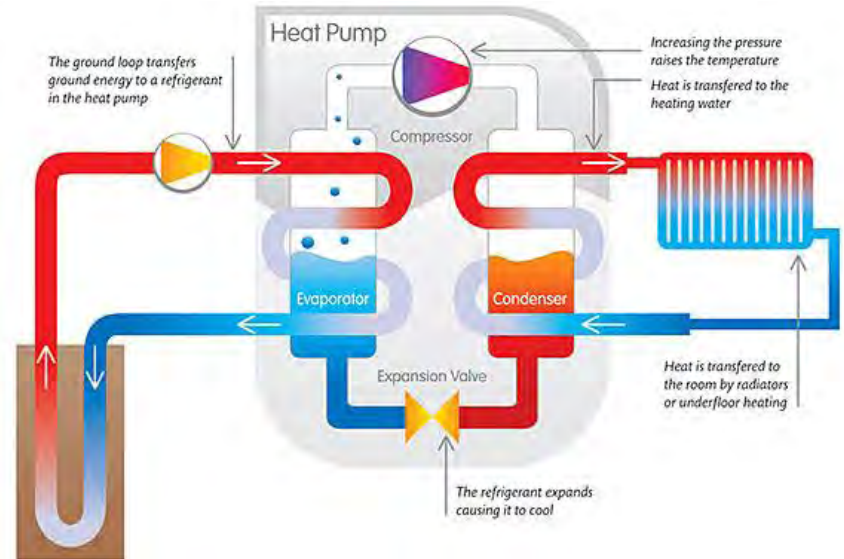


Application 7

Ground energy at Urban Scale

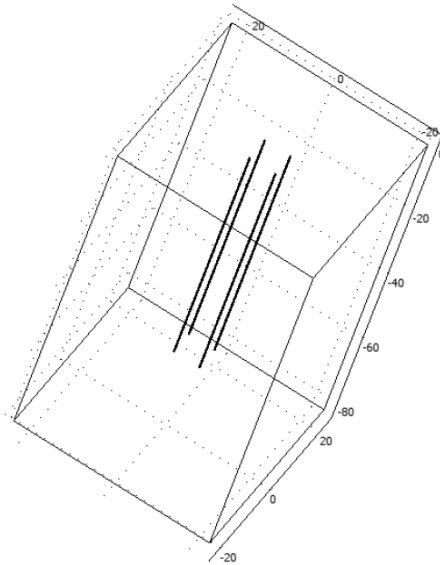
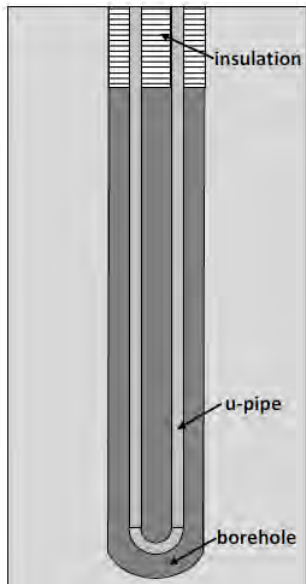


Figure 7.3 Image and location of the Anatomy House in Göteborg (Microsoft, 2010).



Application 7

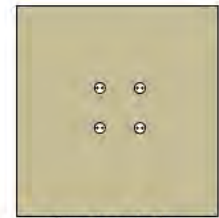
Ground energy at Urban Scale



single borehole



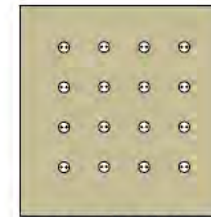
two boreholes



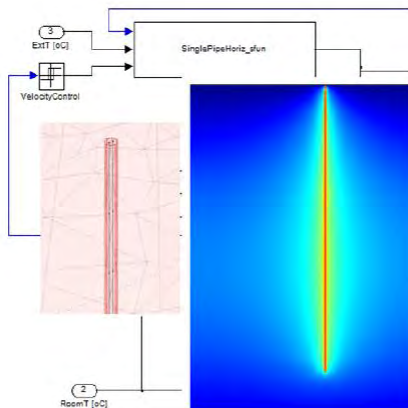
four boreholes



eight boreholes



sixteen boreholes



Thanks to: David van Reenen

Application 7

Ground energy at Urban Scale

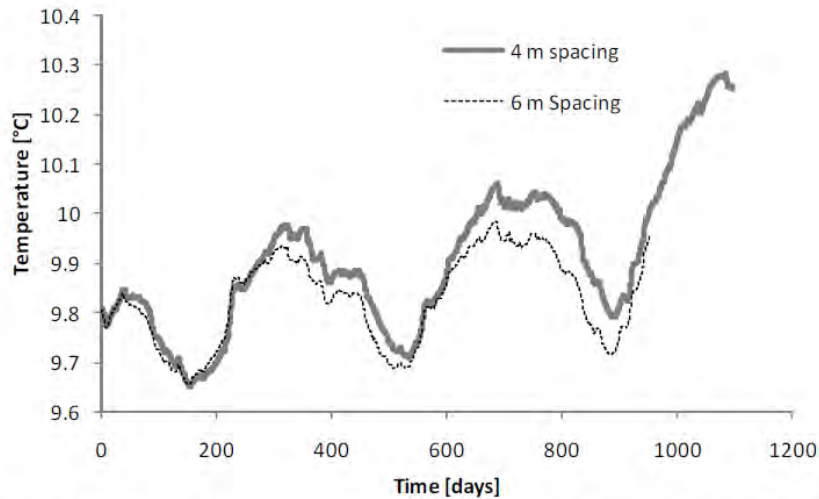


Figure 6.13 Ground temperature at a distance of 2 m from the borehole for the Gothenburg simulations.

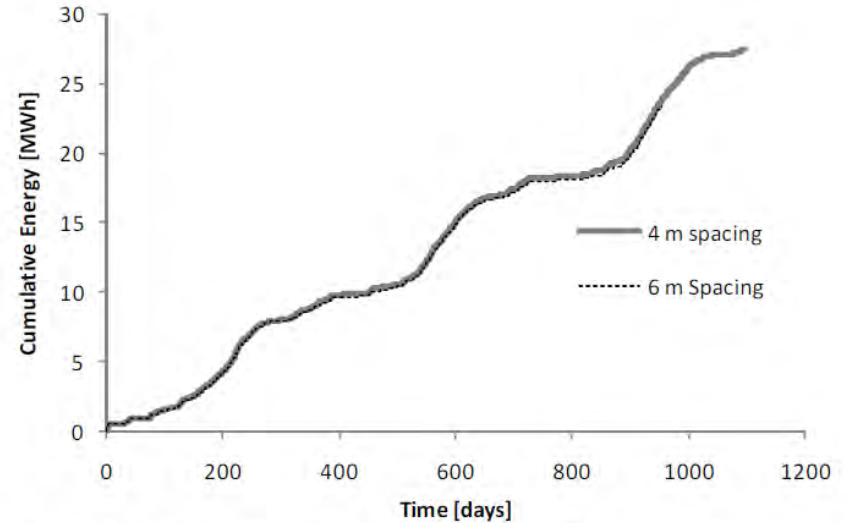
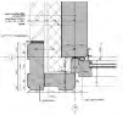


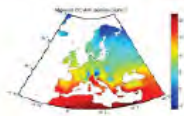


Figure 6.11 Cumulative absolute energy supplied to the building zone for the Gothenburg simulations.

Thanks to: David van Reenen

Computational Building Physics

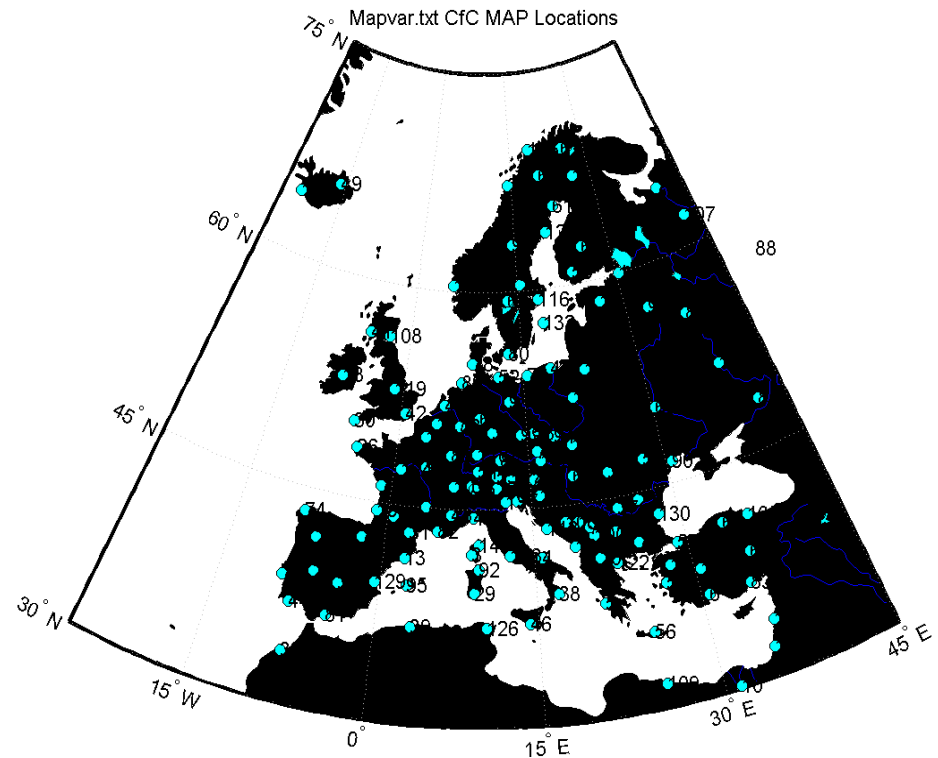
Heat, including EU Scale

Topic \ Scale	Heat	Moisture	Air	Stress
~ mm 				
~ m 				
~ km 				
~ Mm 				

Application 8

Incorporate EU Scale

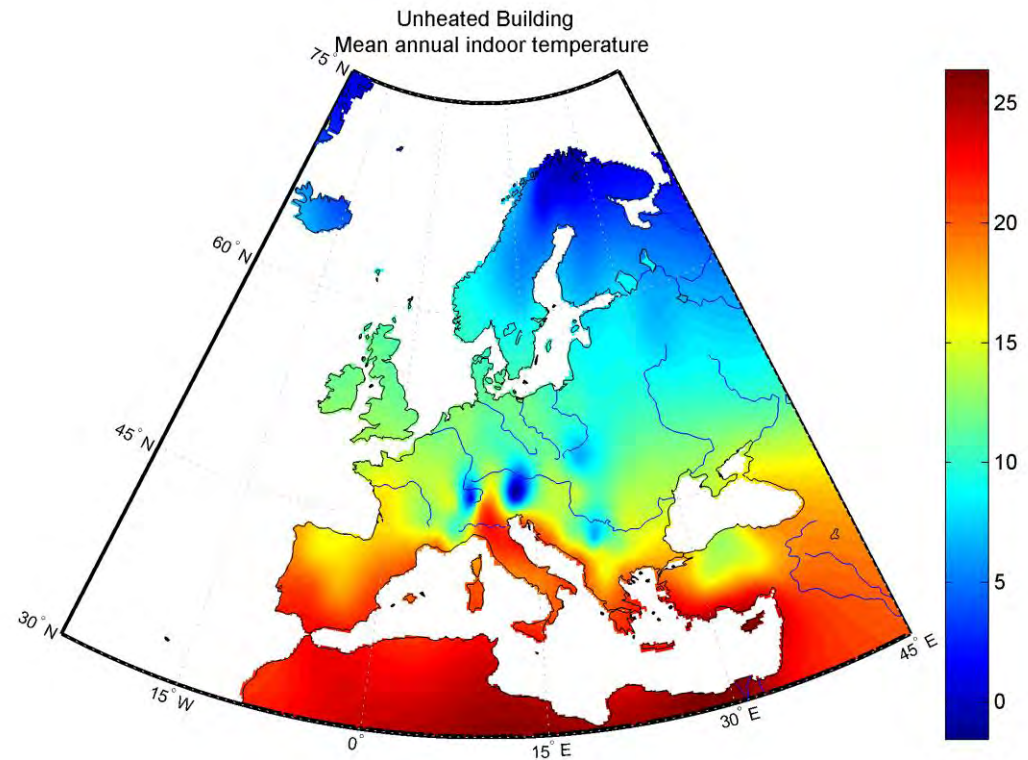
- Weather Stations
- Used as boundary values for the external climate



Application 8

Incorporate EU Scale

- Subject building constructions to external climates
- Map performances



Conclusion

- **COMSOL** is a state-of-art Multiphysics modeling tool for doing research in the area of building physics
- High performance on
 - 1,2 & 3D capabilities
 - Grid & solvers techniques
 - Visualization
 - Flexibility due to PDE abstraction level
- Also an excellent tool for education
- Our models are available at <http://sts.bwk.tue.nl/hamlab/>

- Thank you
- Questions?

